

Balancing the Books

Lisa Lippincott

If your subprogram follows certain rules, it gets a gold star!



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Const correctness in C++

RAII resource management in C++

Borrow/freeze correctness in Rust

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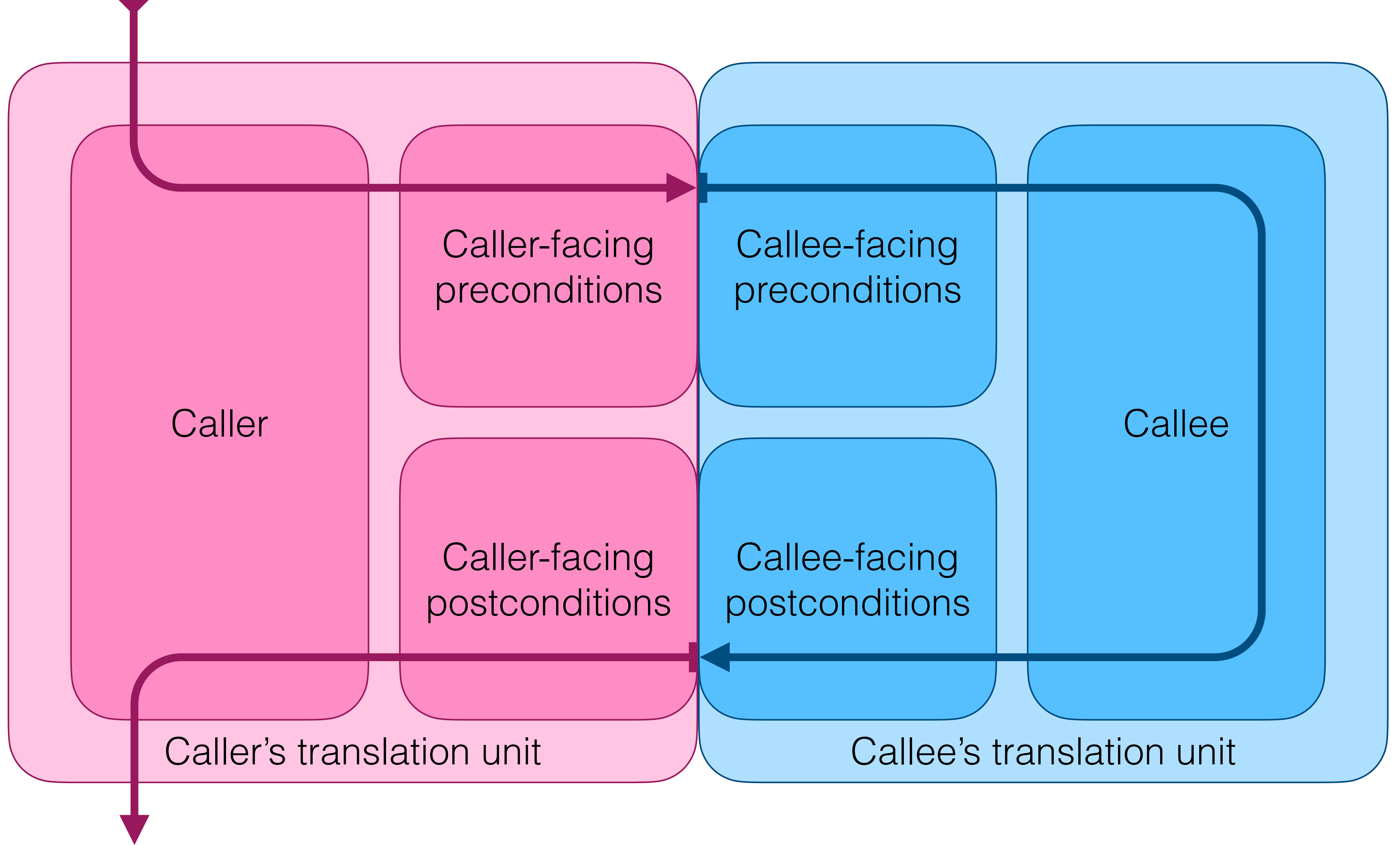


Rust-style borrow/freeze correctness copied into C++

The contracts facility in C++26 does not provide Rust-style borrow/freeze correctness.

But could it in a future version of C++?

- Users choose between efficient trust and redundant verification.
- The choice is made outside the source code.
- The choice is granular, at translation unit scale or smaller.
- The choices made for different translation units are independent.
- At boundaries, either side can insist on verification.



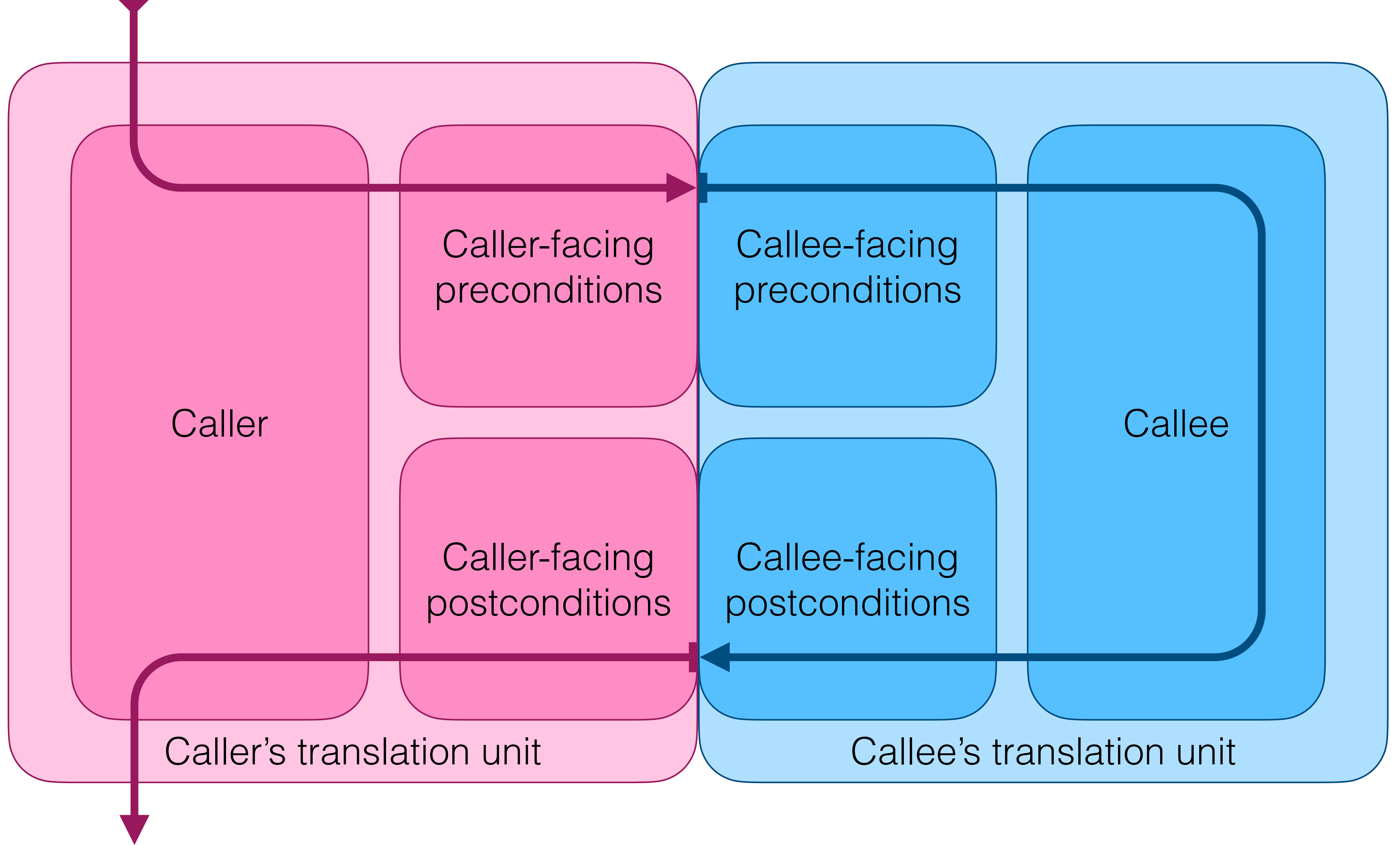
- Assertions are verified by inspecting runtime data.
- The verification is hidden from the code being verified.

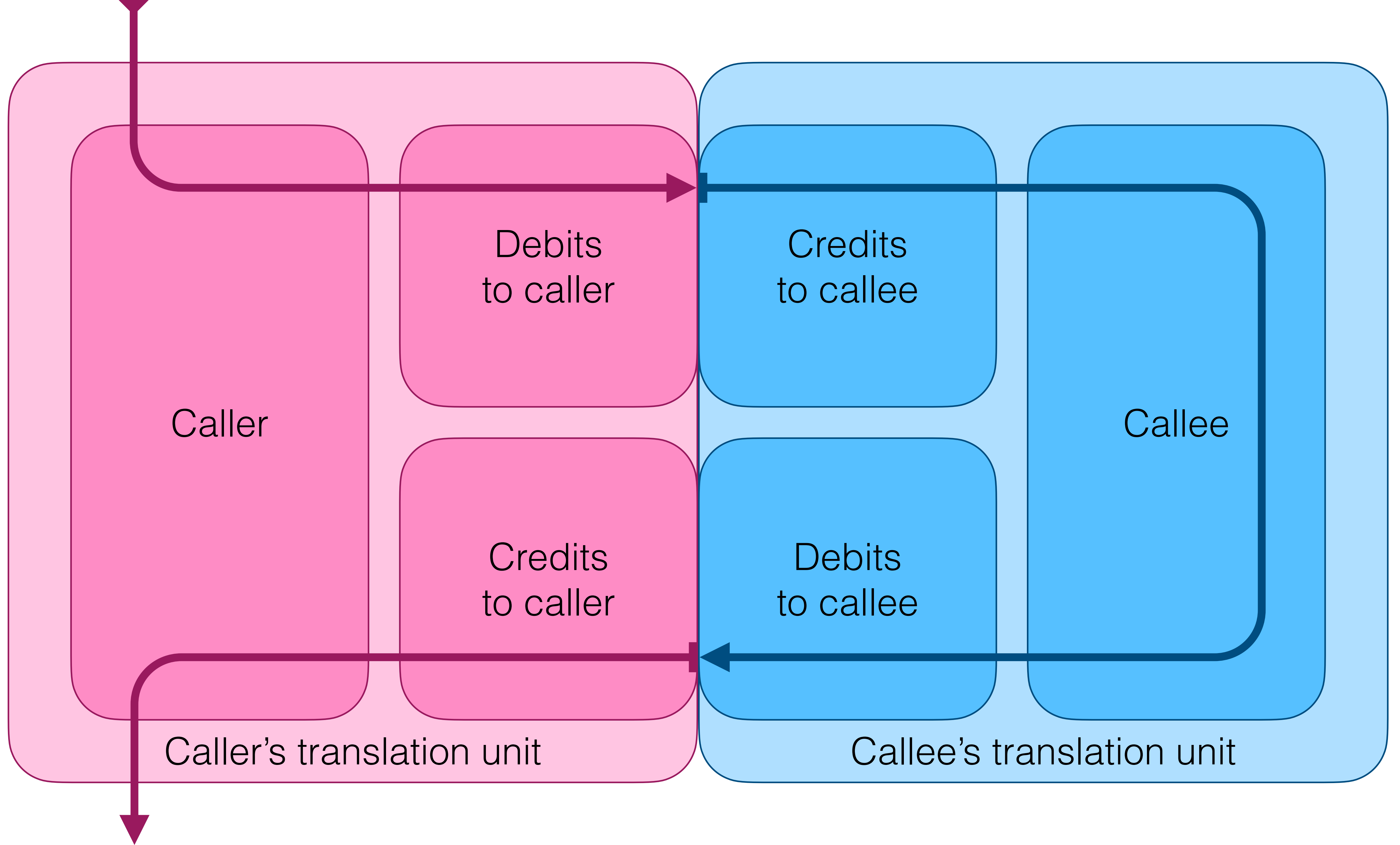
For contract-like verification that goes beyond the values of objects, we need runtime data that is:

- hidden from the code in our translation unit
- not reliant on other translation units
- but can still affect the outcome of verification.

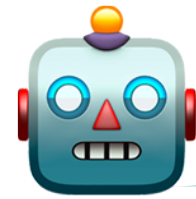
Double-entry bookkeeping

Inventor unknown. Earliest known use 1299.



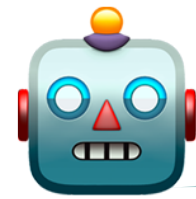
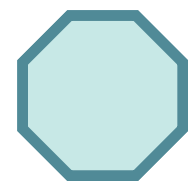


I'd like a variable with the value five, please.



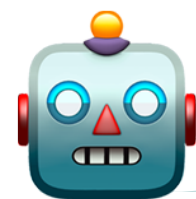
OK, I made a variable. It's value is five.

Can I have some assurance that the value will continue to be five in the future?



I promise it won't change. I give you this token as a symbol of my vow.

What if I grow tired of five, and want a different value?



Return the token to me. I'll change things, and then I'll give you a new token.



Wesley Newcomb Hohfeld (1879-1918)

Some Fundamental Legal Conceptions
as Applied in Judicial Reasoning

Yale Law Journal, 1913





**RETAIN TOKEN
TO PREVENT
CHANGE**

Hohfeldian right

- Prevents change
- Not duplicable
- Transferrable



**RETAIN TOKEN
TO PREVENT
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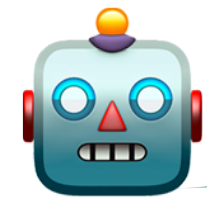
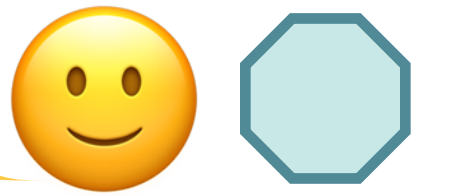
Hohfeldian right

- Prevents change
- Not duplicable
- Transferrable
- Remitted intact to request change



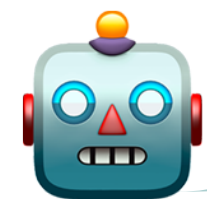
**REMIT TOKEN
TO REQUEST
CHANGE**

Tell me the value of my variable, please.



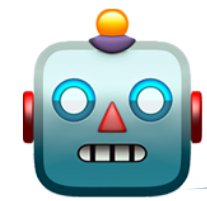
Did I say it had a stable value?

Oh yes, you gave me a token as symbol.



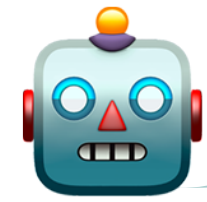
Show me, please.

But if I give you back the token you gave me, you could change the value.



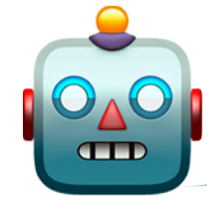
I see. Bit of a conundrum, that.

Tell me the value of my variable, please.



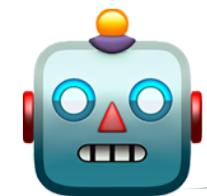
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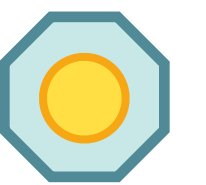
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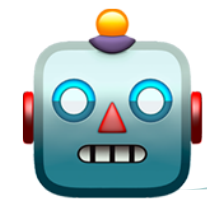
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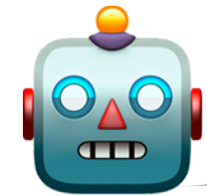
I'll make a new token for you out of a little piece of the one you gave me.





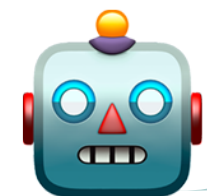
Did I say it had a stable value?

Oh yes, you gave me a token as symbol.



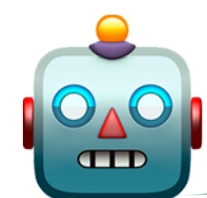
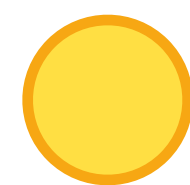
Show me, please.

But if I give you back the token you gave me, you could change the value.



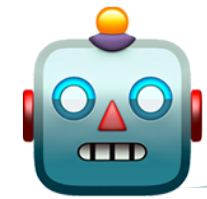
I see. Bit of a conundrum, that.

I'll make a new token for you out of a little piece of the one you gave me.



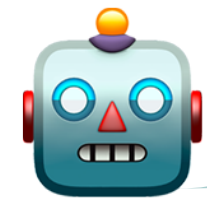
Excellent. Here's your value, and here's your token back.

Oh yes, you gave me a token as symbol.



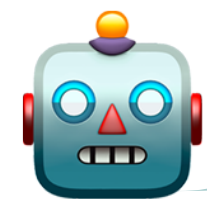
Show me, please.

But if I give you back the token you gave me, you could change the value.



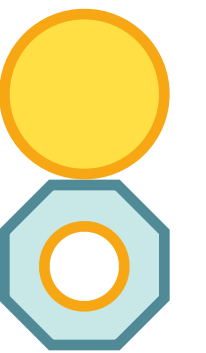
I see. Bit of a conundrum, that.

I'll make a new token for you out of a little piece of the one you gave me.



Excellent. Here's your value, and here's your token back.

Thanks! I'll fill in the hole now.





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- Not valid for change requests



**NOT VALID
FOR CHANGE
REQUESTS**



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Hohfeldian immunity

- Prevents change
- Not duplicable
- Transferrable only to issuer
- Not valid for change requests



Hohfeldian right

- Prevents change
- Not duplicable
- Transferrable
- Remitted intact to request change
- May issue immunities by taking on disabilities



Hohfeldian immunity

- Prevents change
- Not duplicable
- Transferrable only to issuer
- Not valid for change requests
- May issue further immunities by taking on disabilities

```
void swap( int& a, int& b )  
{  
    int c;  
    c = a;  
    a = b;  
    b = c;  
}
```


	Credits	Debits	Balance
<i>// provided by caller</i>	 		

```
int c;  
c = a;  
a = b;  
b = c;
```

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 

```

int c;
c = a;
a = b;
b = c;

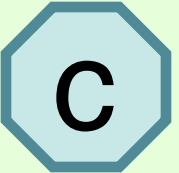
```

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			

```

c = a;
a = b;
b = c;

```

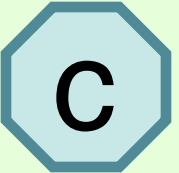

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			  

c = a;
a = b;
b = c;

	Credits	Debits	Balance
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<code>int c;</code>			  
<code>c = a;</code>		 	

`a = b;`

`b = c;`

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
<code>int c;</code>			  
<code>c = a;</code>		 	 

`a = b;`

`b = c;`

	Credits	Debits	Balance
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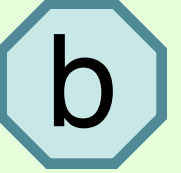
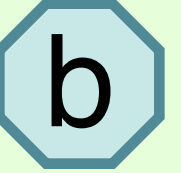
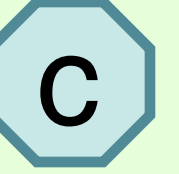
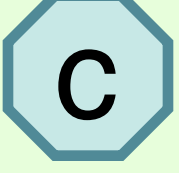
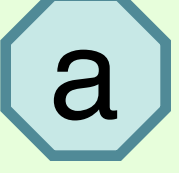
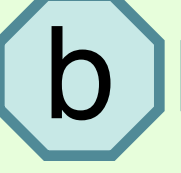
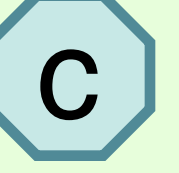
`a = b;`

`b = c;`

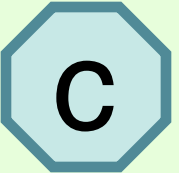
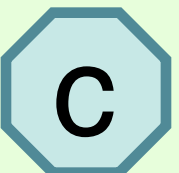
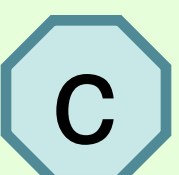
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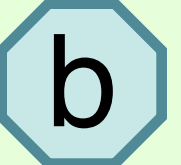
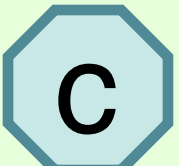
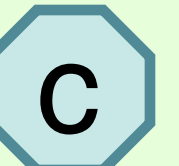
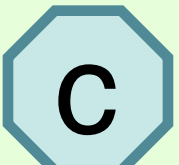
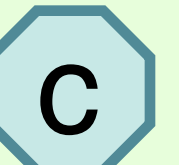
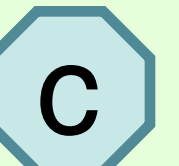
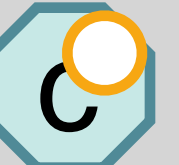
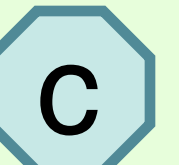
b = c;

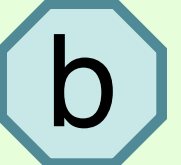
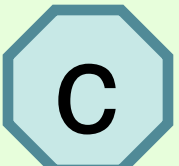
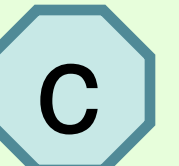
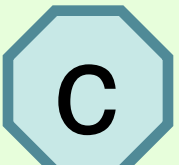
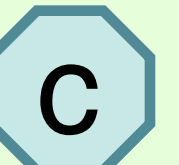
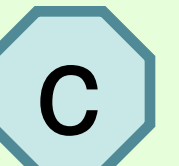
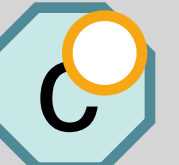
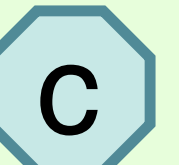
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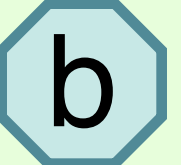
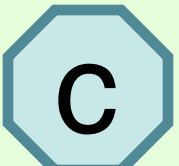
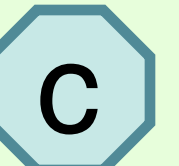
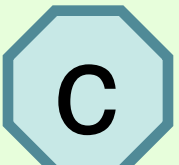
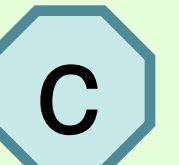
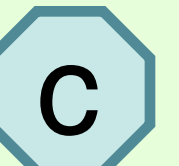
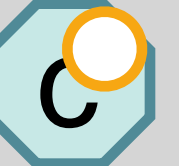
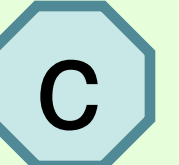
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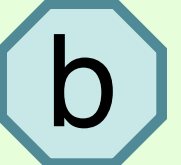
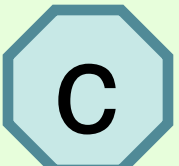
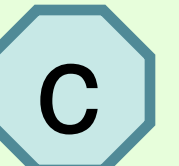
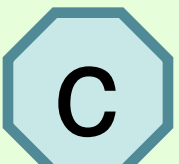
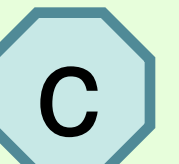
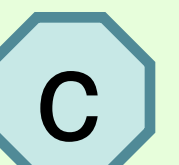
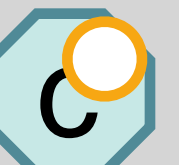
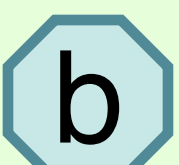
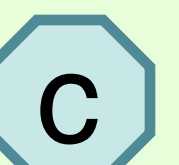
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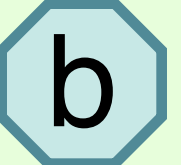
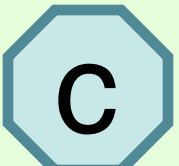
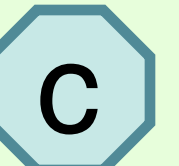
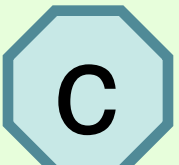
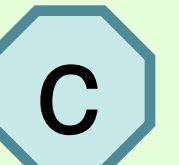
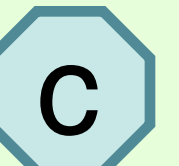
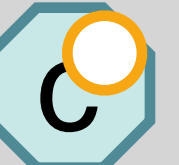
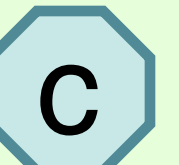
b = c;

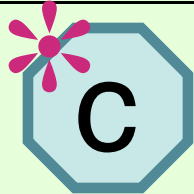
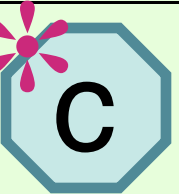
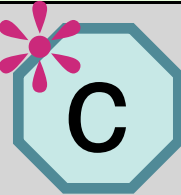
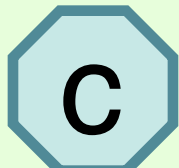
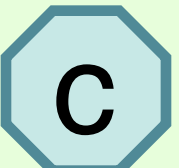
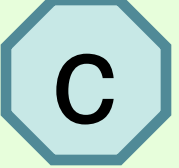
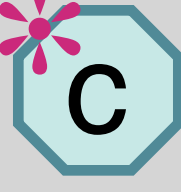
	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			  
c = a;	 		 
	 		  
a = b;	 		 
	 		  
b = c;	 		 
	 		  

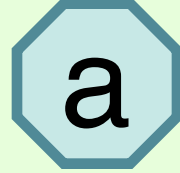
	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			  
c = a;		 	 
	 		  
a = b;		 	 
	 		  
b = c;		 	 
	 		  
<i>// end of local scope</i>			

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			  
c = a;		 	 
	 		  
a = b;		 	 
	 		  
b = c;		 	 
	 		  
<i>// end of local scope</i>			 

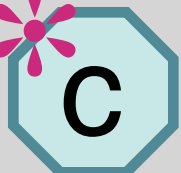
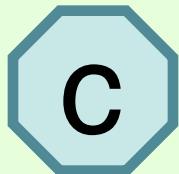
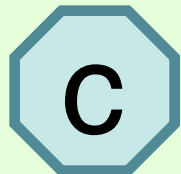
	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
<code>int c;</code>			  
<code>c = a;</code>		 	 
	 		  
<code>a = b;</code>		 	 
	 		  
<code>b = c;</code>		 	 
	 		  
<i>// end of local scope</i>			 
<i>// returned to caller</i>		 	

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			  
c = a;		 	 
	 		  
a = b;		 	 
	 		  
b = c;		 	 
	 		  
<i>// end of local scope</i>			 
<i>// returned to caller</i>		 	

	Credits	Debits	Balance
<i>// provided by caller</i>	 		 
int c;			  
c = a;		 	 
	 		  
a = b;		 	 
	 		  
b = c;		 	 
	 		  
<i>// end of local scope</i>			 
<i>// returned to caller</i>		 	

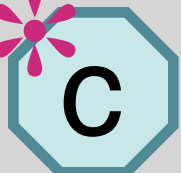
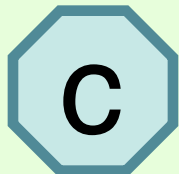
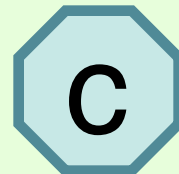
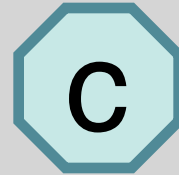
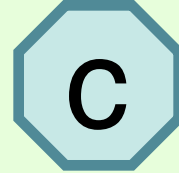
	Credits	Debits	Balance
<i>// provided by caller</i>			

```
int c;  
c = a;  
a = b;  
b = c;
```

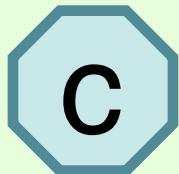
	Credits	Debits	Balance
<i>// provided by caller</i>			
int c;	 		  
c = a;	  		 
	 		 

a = b;

b = c;

	Credits	Debits	Balance
<i>// provided by caller</i>			
int c;	 		  
c = a;	  		 
	 		 
a = b;			
			 

b = c;

	Credits	Debits	Balance
<i>// provided by caller</i>			
int c;	 		  
c = a;	  		 
	 		 
a = b;			
			 
b = c;	  		 
	 		 

	Credits	Debits	Balance
<i>// provided by caller</i>			
<code>int c;</code>			
<code>c = a;</code>			
<code>a = b;</code>			
<code>b = c;</code>			
<i>// end of local scope</i>			
<i>// returned to caller</i>			


```
void swap( int& a, int& b )
```

```
interface
```

```
{
```

```
if ( &a != &b )
```

```
{
```

```
transfer a, b;
```

Two object rights transferred

```
implementation;
```

```
transfer a, b;
```

Two object rights returned

```
}
```

```
else
```

```
{
```

```
transfer a;
```

One object right transferred

```
transfer_reference b = a;
```

```
implementation;
```

```
transfer a;
```

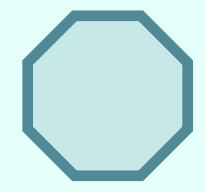
One object right returned

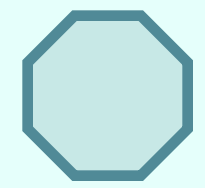
```
}
```

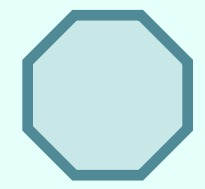
```
}
```

```
void swap( int& a, int& b )
interface
{
    if ( &a != &b )
    {
        transfer a, b;
        implementation;
        transfer a, b;
    }
    else
    {
        transfer a;
        transfer_reference b = a;
        implementation;
        transfer a;
    }
}
```

```
int& operator=( int& a, const int& b )
interface
{
    if ( &a != &b )
    {
        transfer a(maybe_uninitialized), const b;
        implementation;
        transfer a, const b;
    }
    else
    {
        transfer a;
        transfer_reference b = a;
        implementation;
        transfer a;
    }
    transfer_reference result = a;
}
```

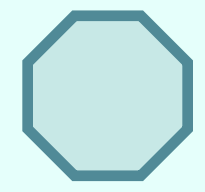
 value of **a**

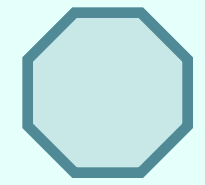
 value of **b**

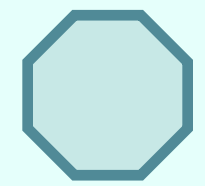
 value of **c**

initialization:

initialized or
maybe_uninitialized

 value of **a**

 value of **b**

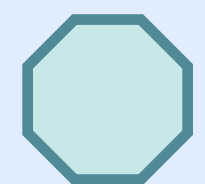
 value of **c**

initialization:

initialized or
maybe_uninitialized

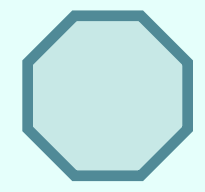
 lifetime of **a**

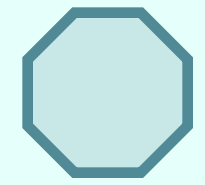
 lifetime of **b**

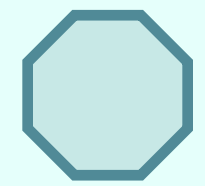
 lifetime of **c**

mutability:

not_declared_const or
maybe_declared_const

 value of **a**

 value of **b**

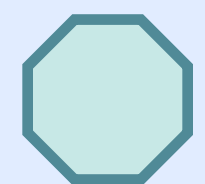
 value of **c**

initialization:

initialized or
maybe_uninitialized

 lifetime of **a**

 lifetime of **b**

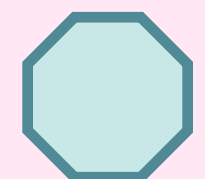
 lifetime of **c**

mutability:

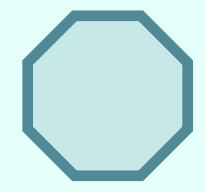
not_declared_const or
maybe_declared_const

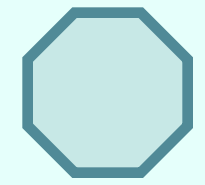
 storage for **a**

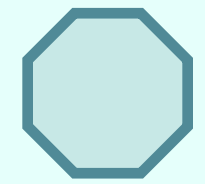
 storage for **b**

 storage for **c**

storage boundary: [begin, end)

 value of **a**

 value of **b**

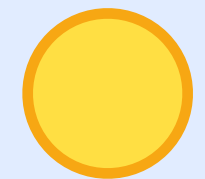
 value of **c**

initialization:

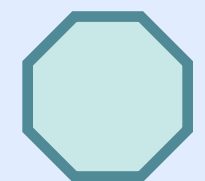
initialized or
maybe_uninitialized

referent:

ledger column + generation

 lifetime of **a**

 lifetime of **b**

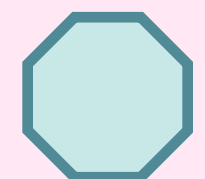
 lifetime of **c**

mutability:

not_declared_const or
maybe_declared_const

 storage for **a**

 storage for **b**

 storage for **c**

storage boundary: [begin, end)


```
void iter_swap( int *a, int *b )
{
    swap( *a, *b );
}
```

```
void reverse( int *a, int *b )
{
    auto p = a, q = b;
    while ( p != q )
    {
        --q;
        if ( p == q )
            break;
        iter_swap( p, q );
        ++p;
    }
}
```

```
void iter_swap( int *a, int *b )
```

```
interface
```

```
{
```

```
  if ( a != b )
```

```
  {
```

```
    int& sa = *a, sb = *b;
```

```
    transfer sa, sb, a = &sa, b = &sb;
```

```
    implementation;
```

```
    transfer sa, sb, a, b;
```

```
  }
```

```
else
```

```
{
```

```
  int& sa = *a;
```

```
  transfer sa, a = &sa, b = &sa;
```

```
  implementation;
```

```
  transfer sa, a, b;
```

```
}
```

```
}
```

The pointers **a** and **b** point into the same ledger columns as **&sa** and **&sb**, respectively.

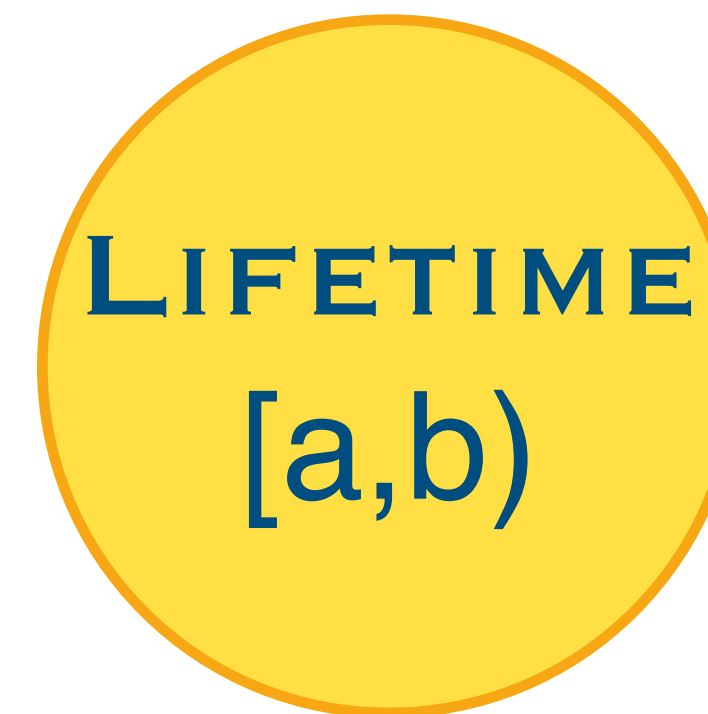
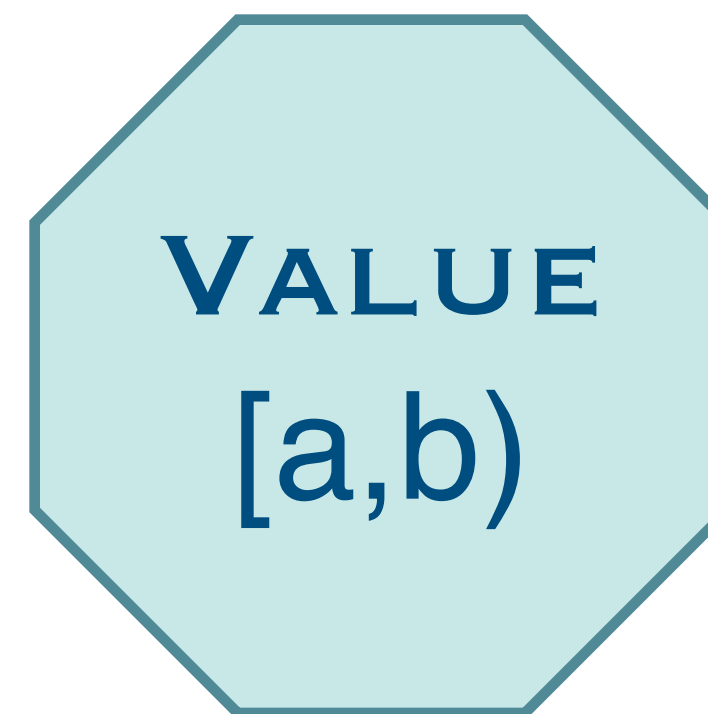
The pointers **a** and **b** both point to the same ledger column as **&sa**.


```
void reverse( int *a, int *b )  
interface  
{  
    const span_ref s( a, b );
```

```
    transfer s,  
        a = s.begin(),  
        b = s.end();
```

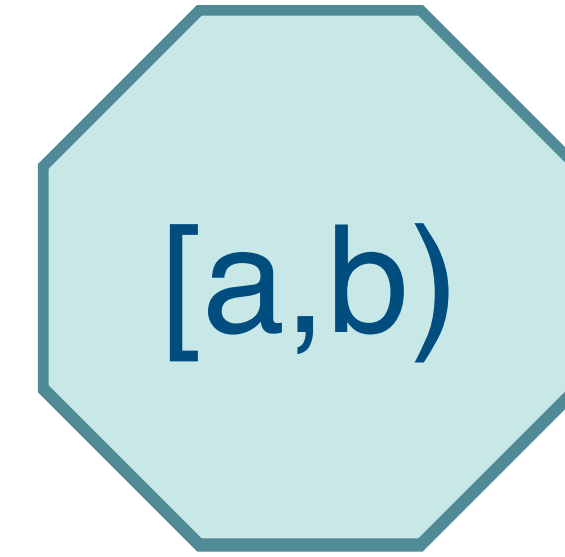
```
implementation;  
  
transfer s, a, b;  
}
```

The referents of bulk reference types like `span_ref` are transferred as bulk tokens.

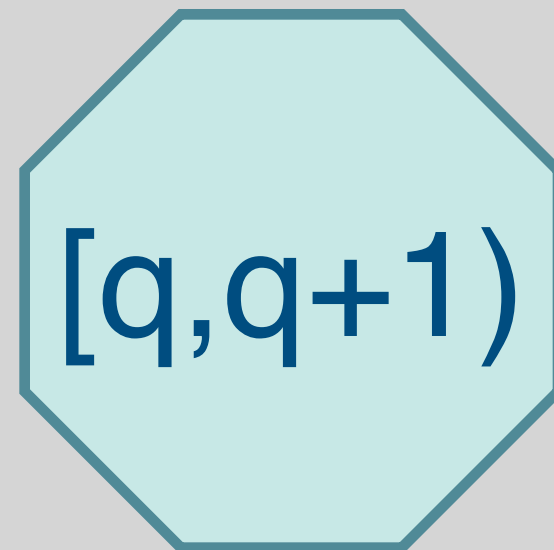
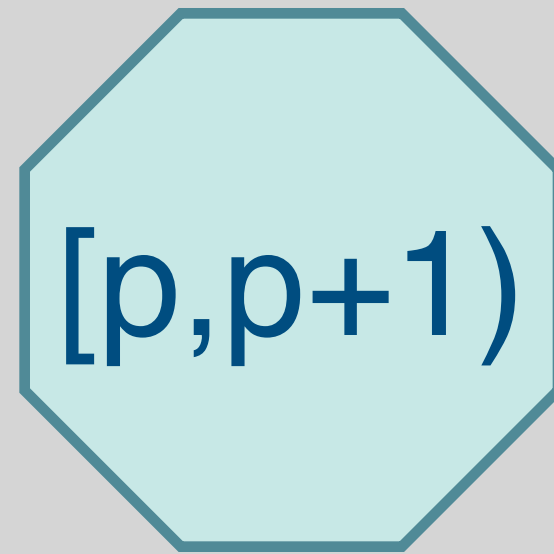


Debits

Balance

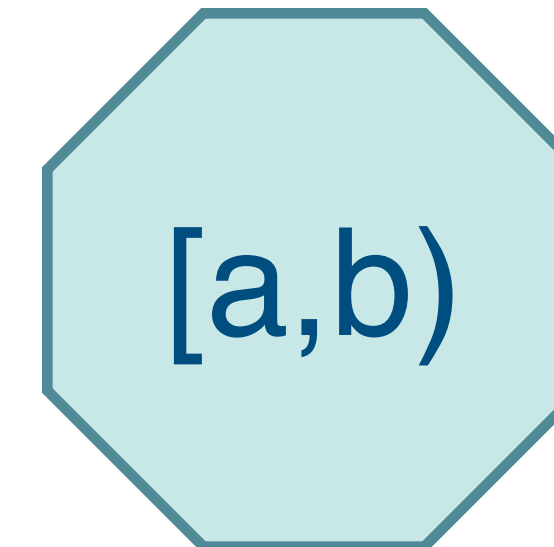


`iter_swap( p, q );`

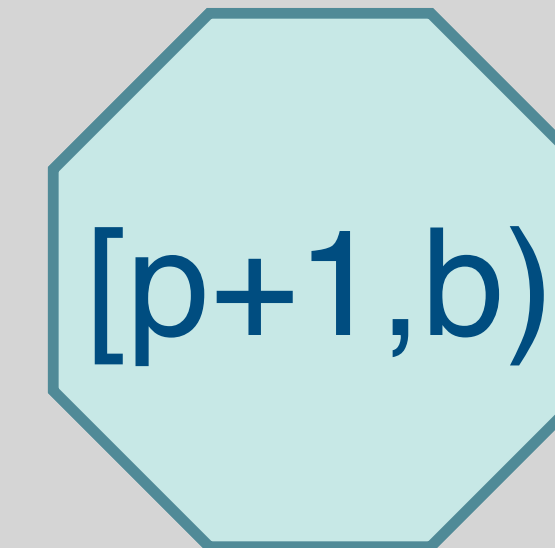
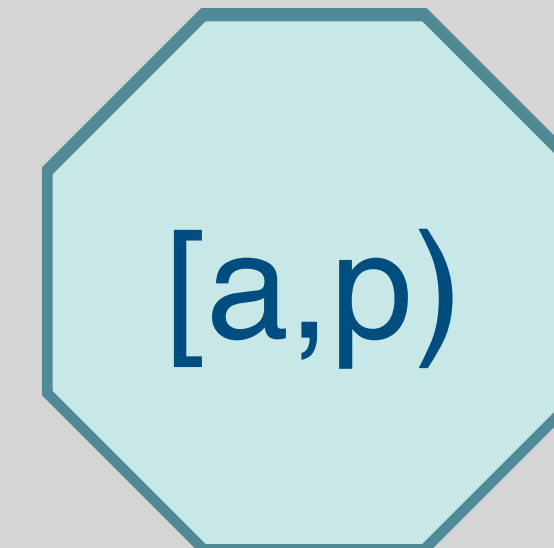
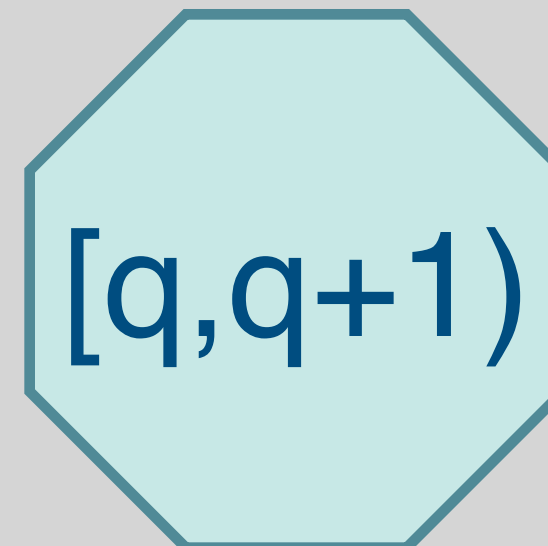
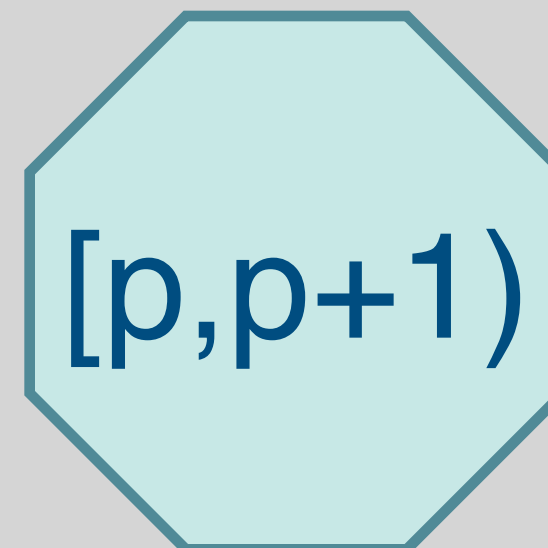


Debits

Balance

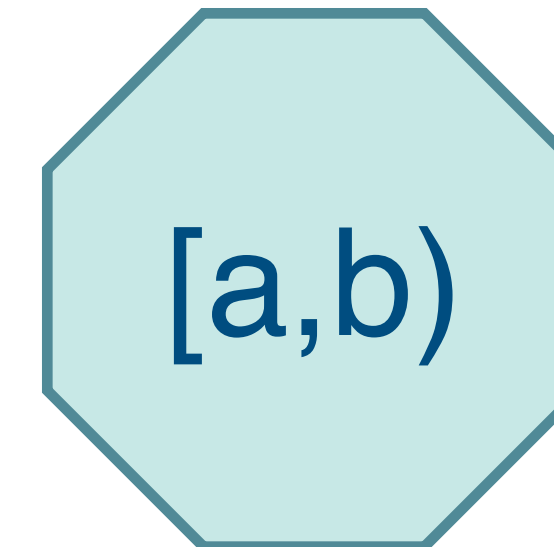


iter_swap(p, q);

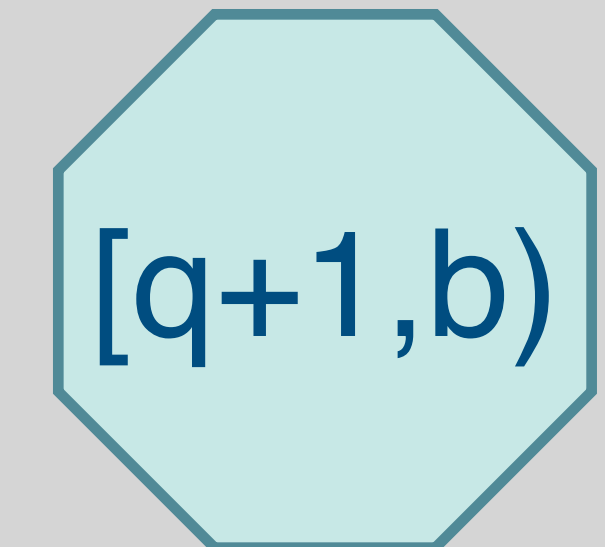
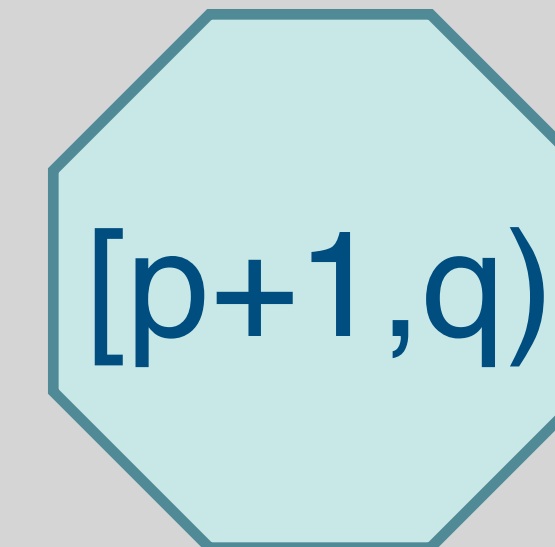
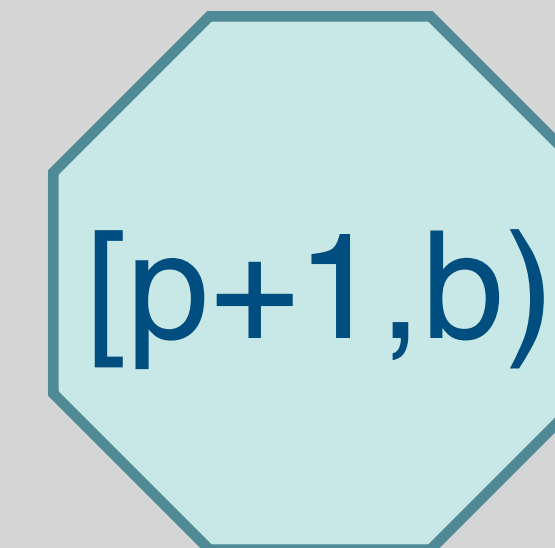
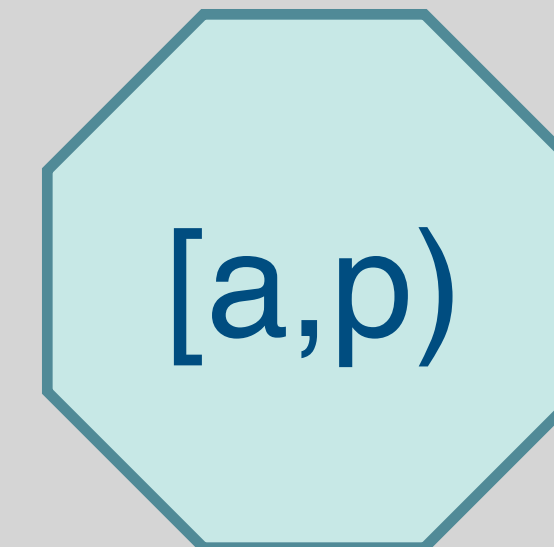
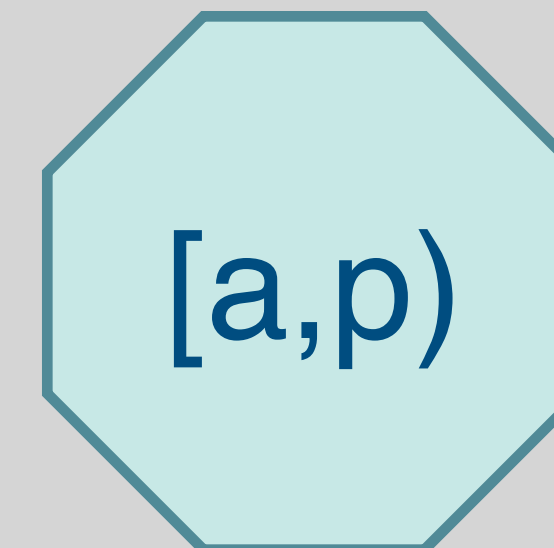
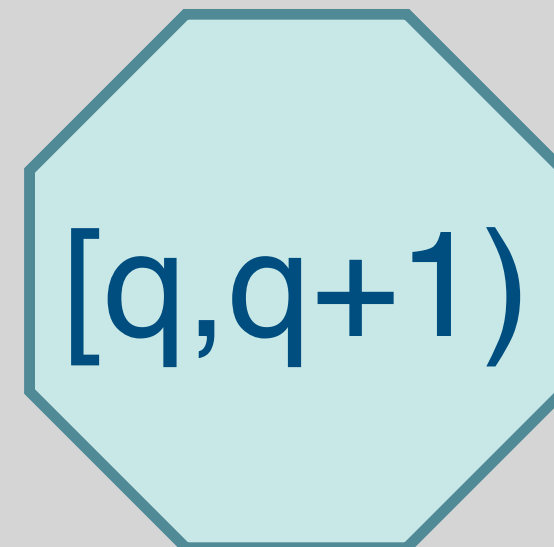
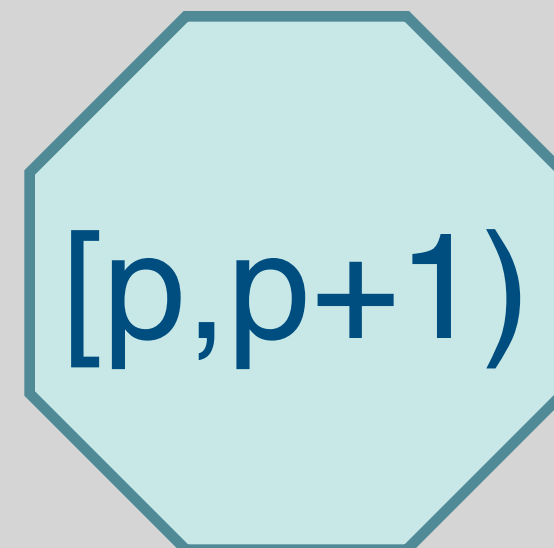


Debits

Balance



iter_swap(p, q);



Debits

Balance



++p;



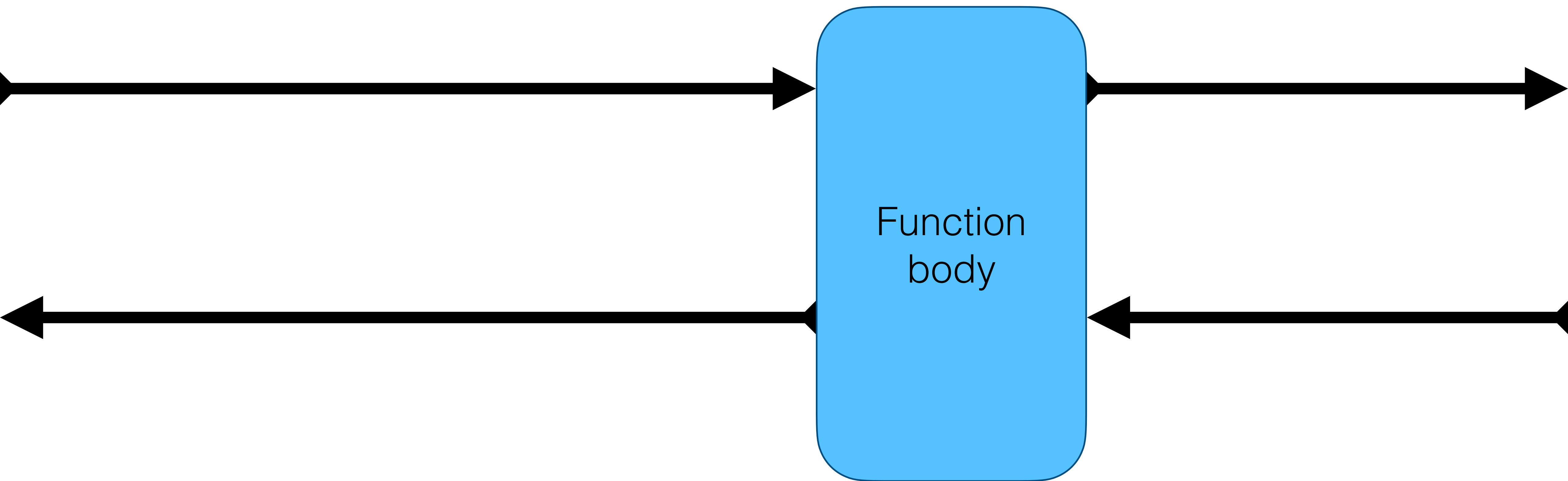
Debits

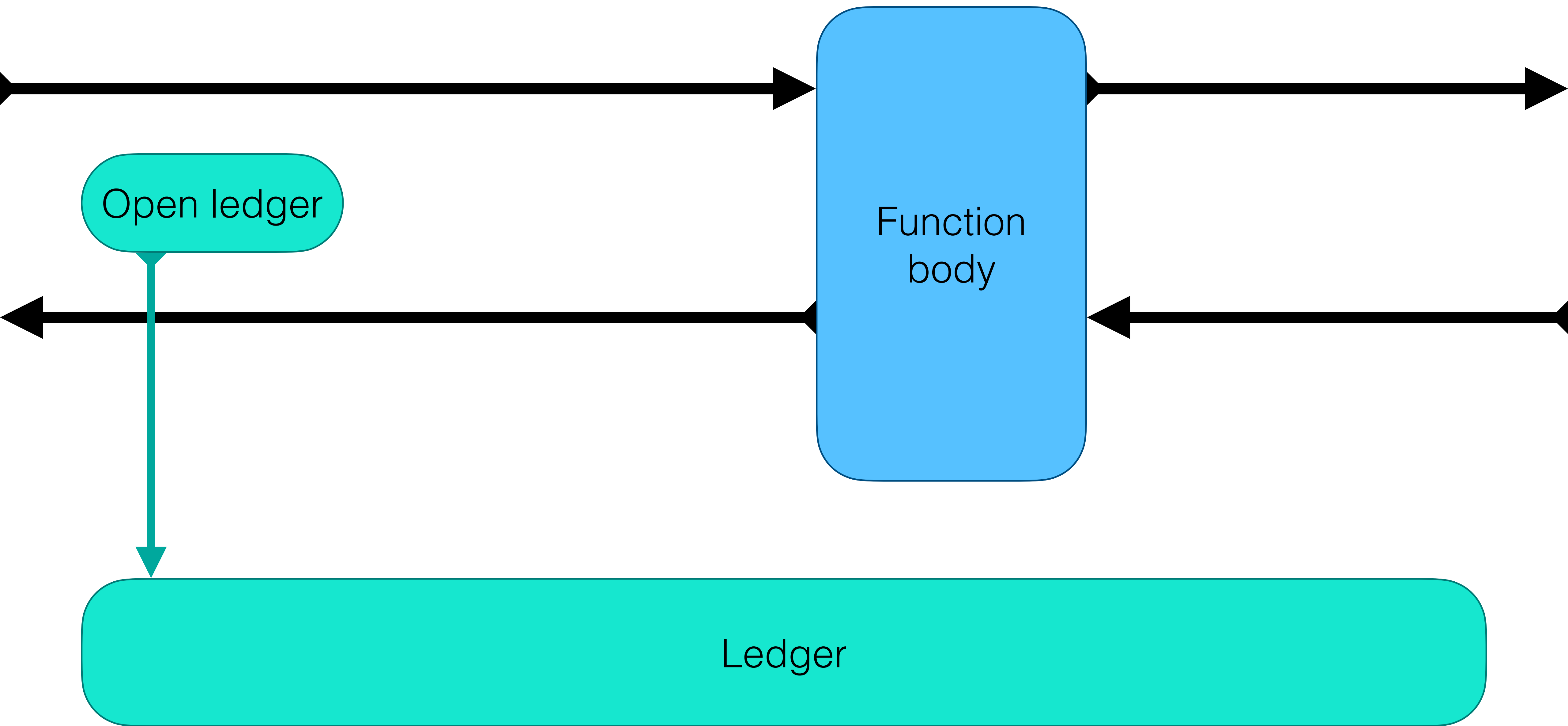
Balance

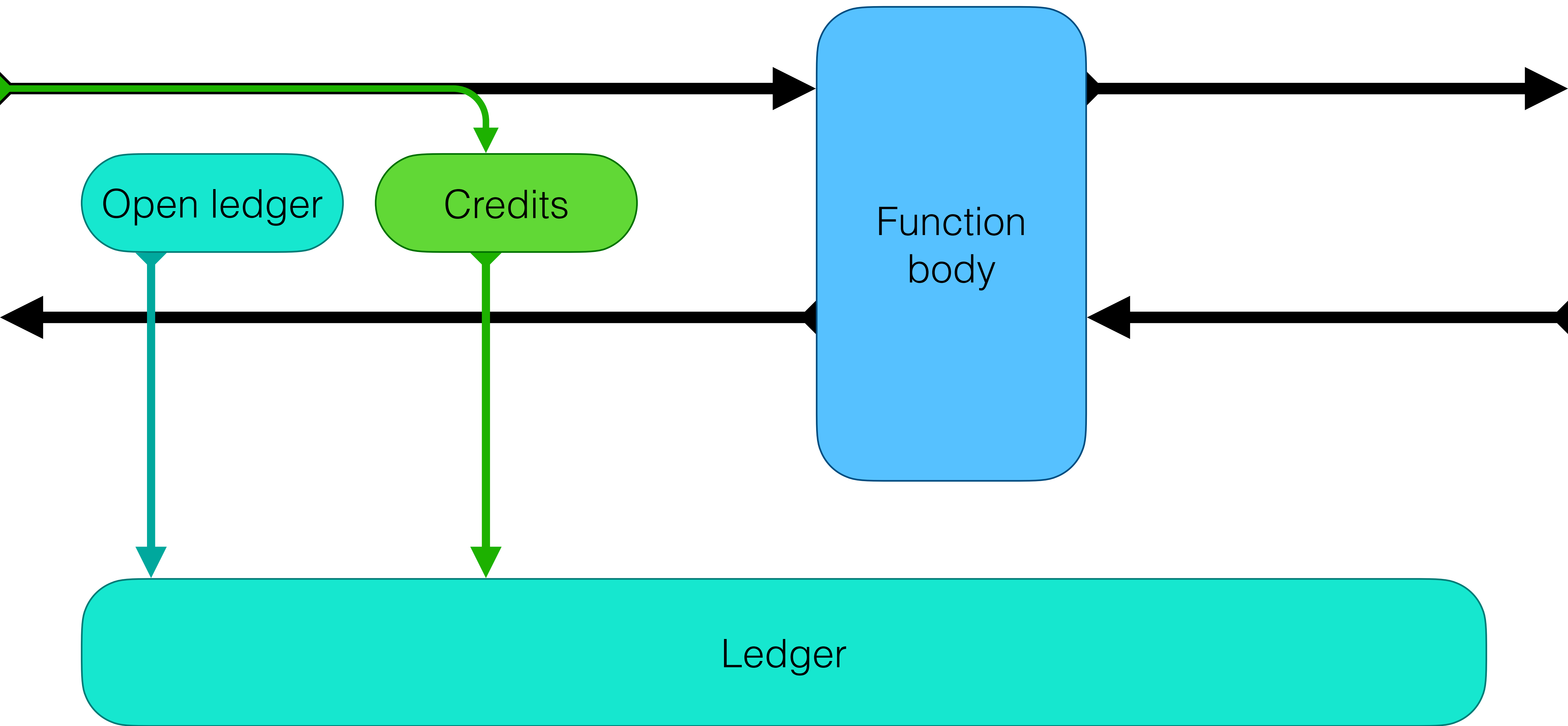


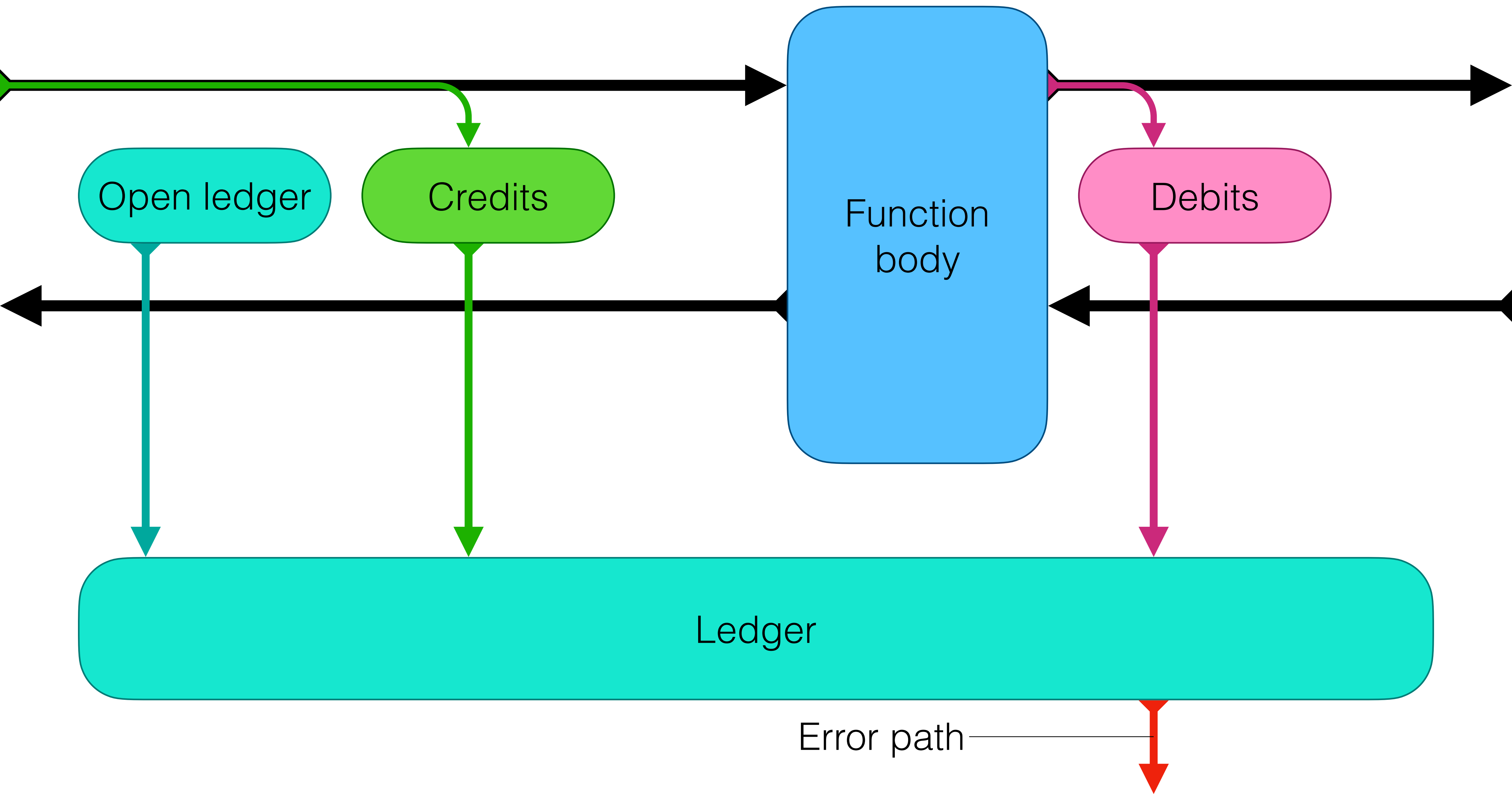
++p;

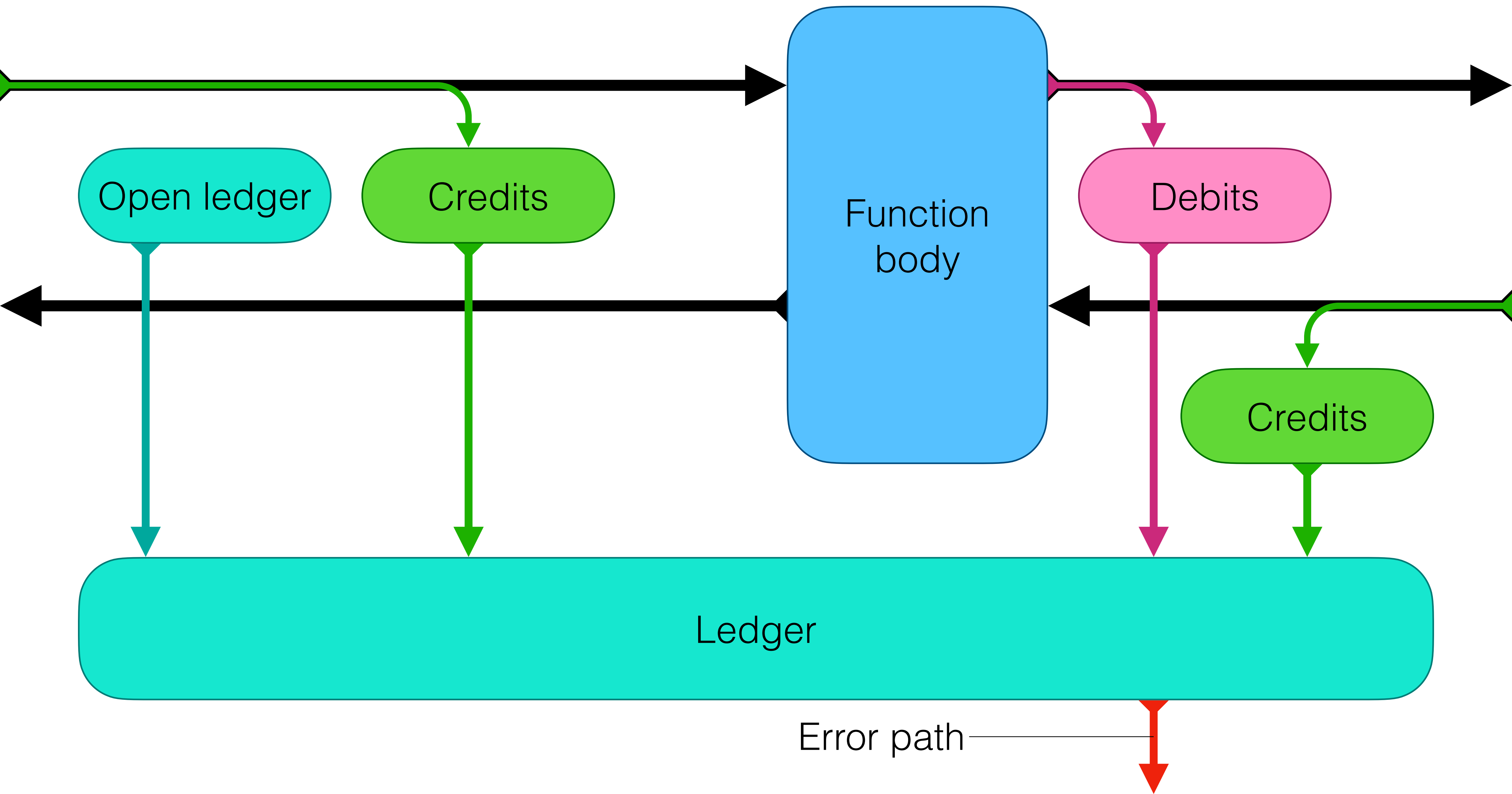


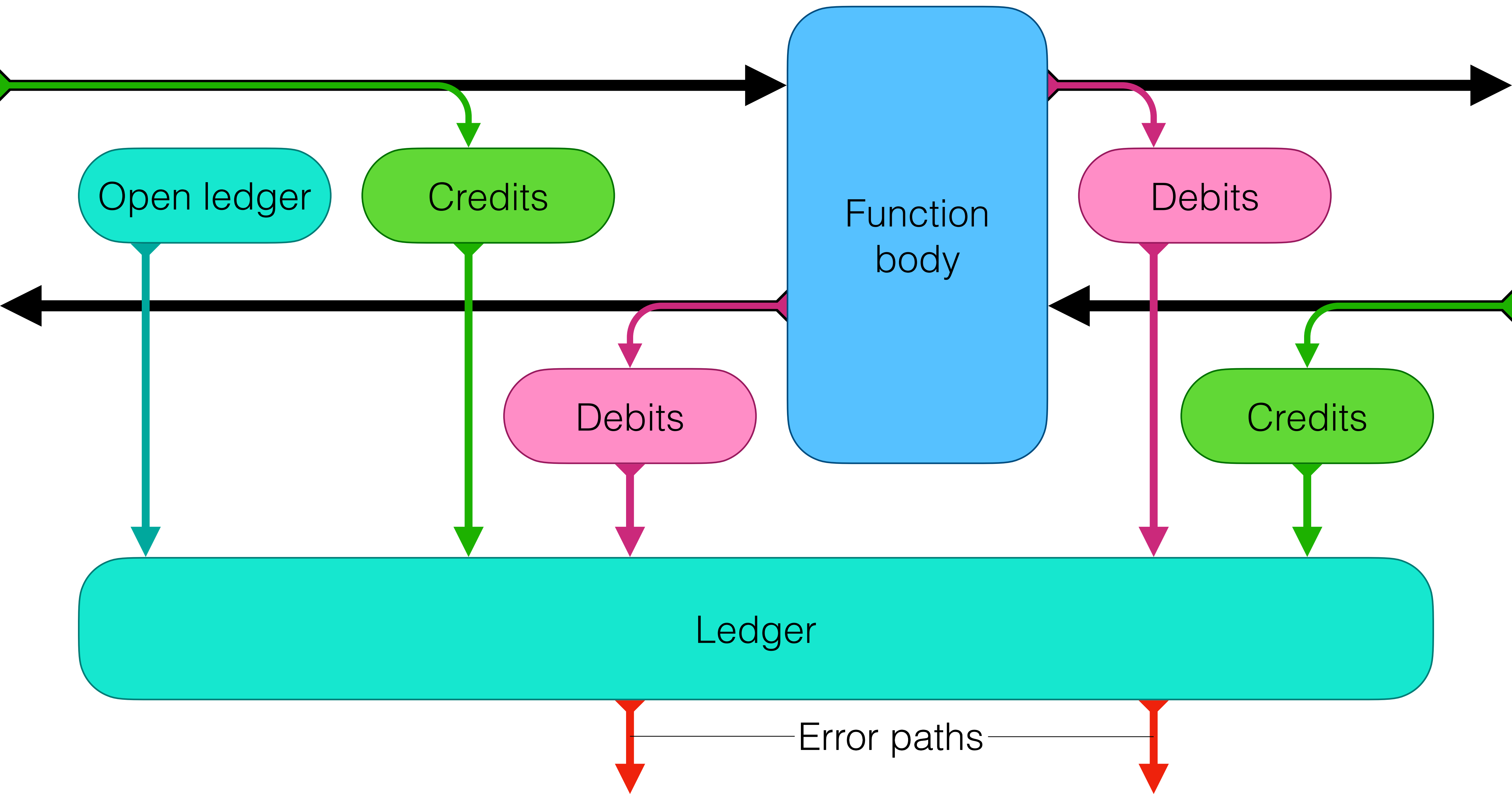


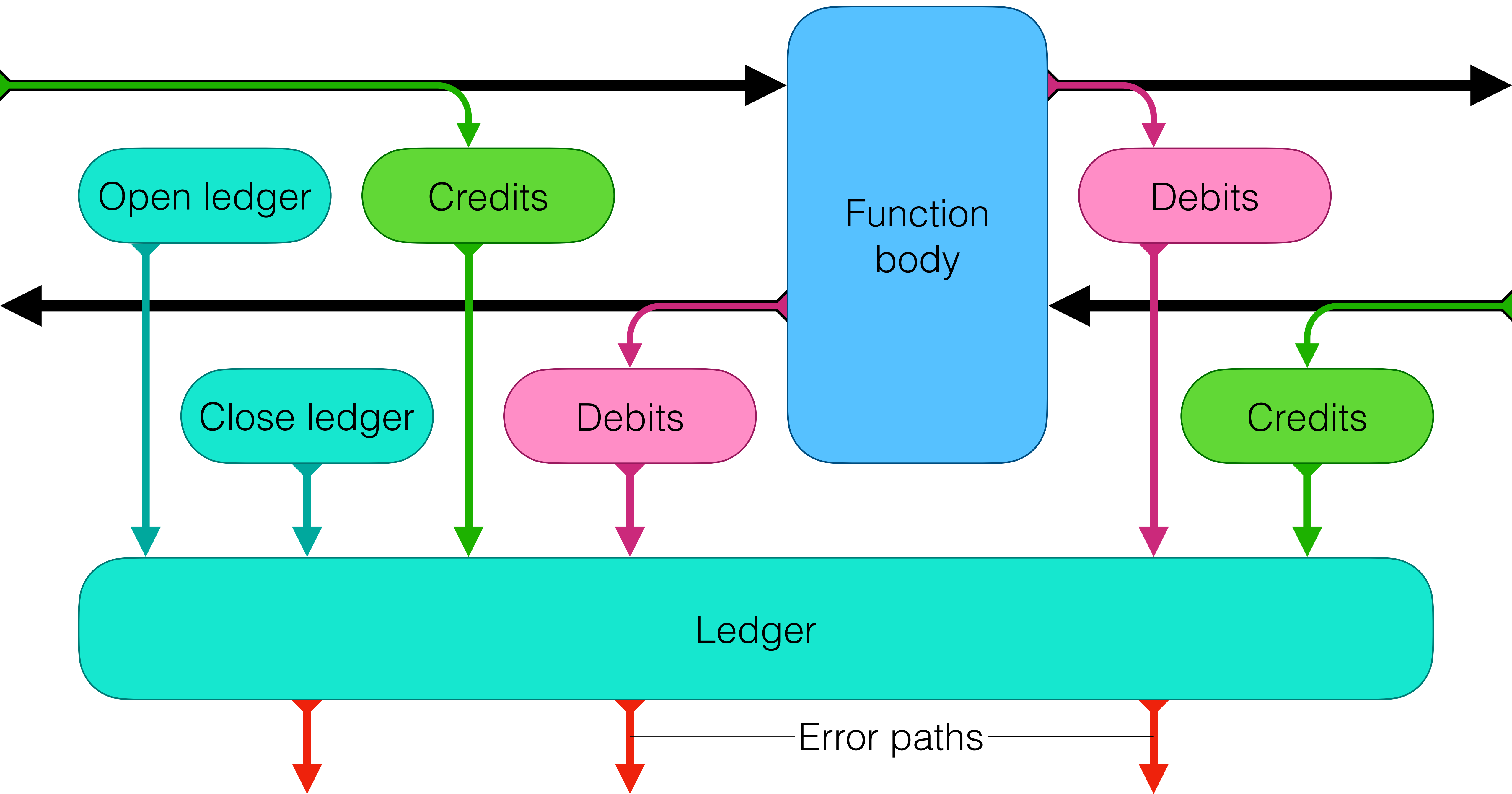


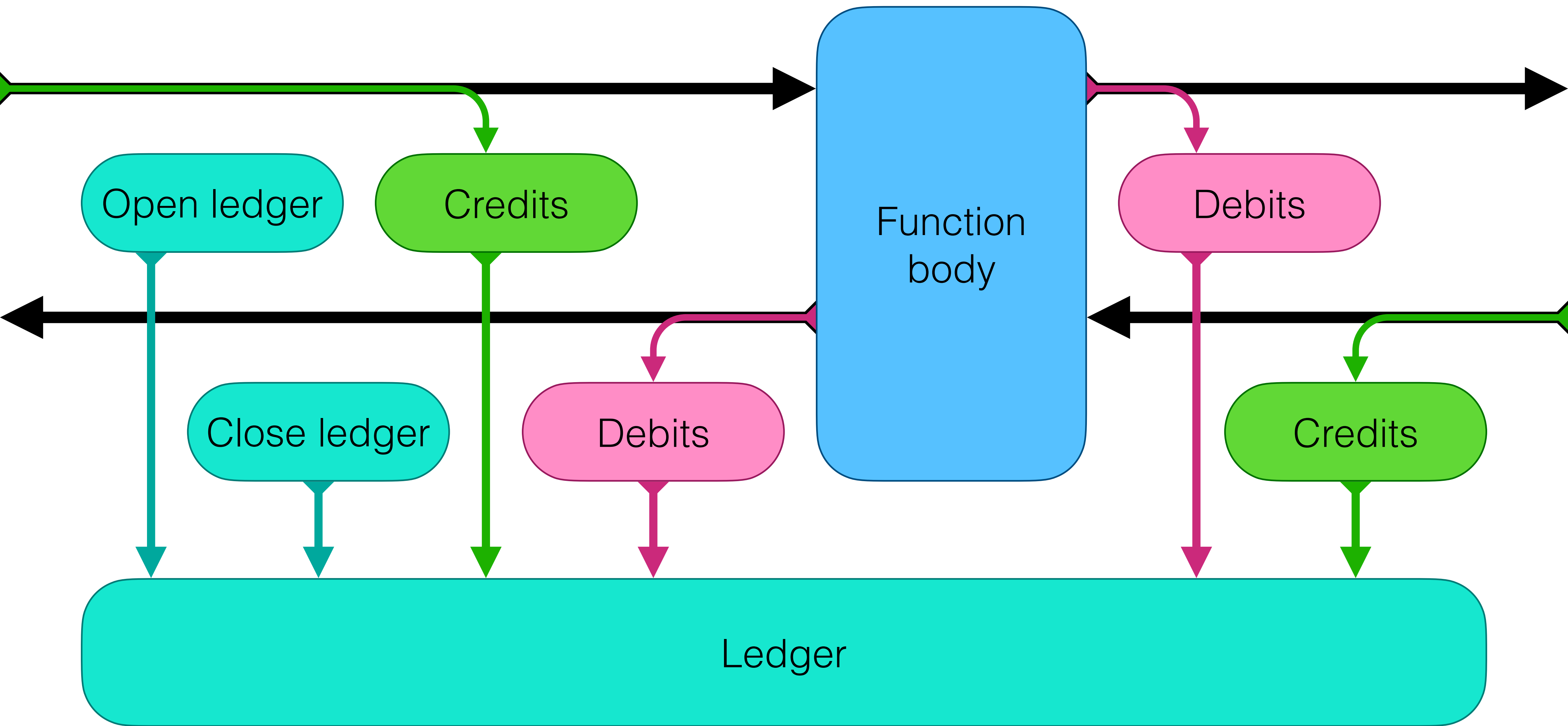


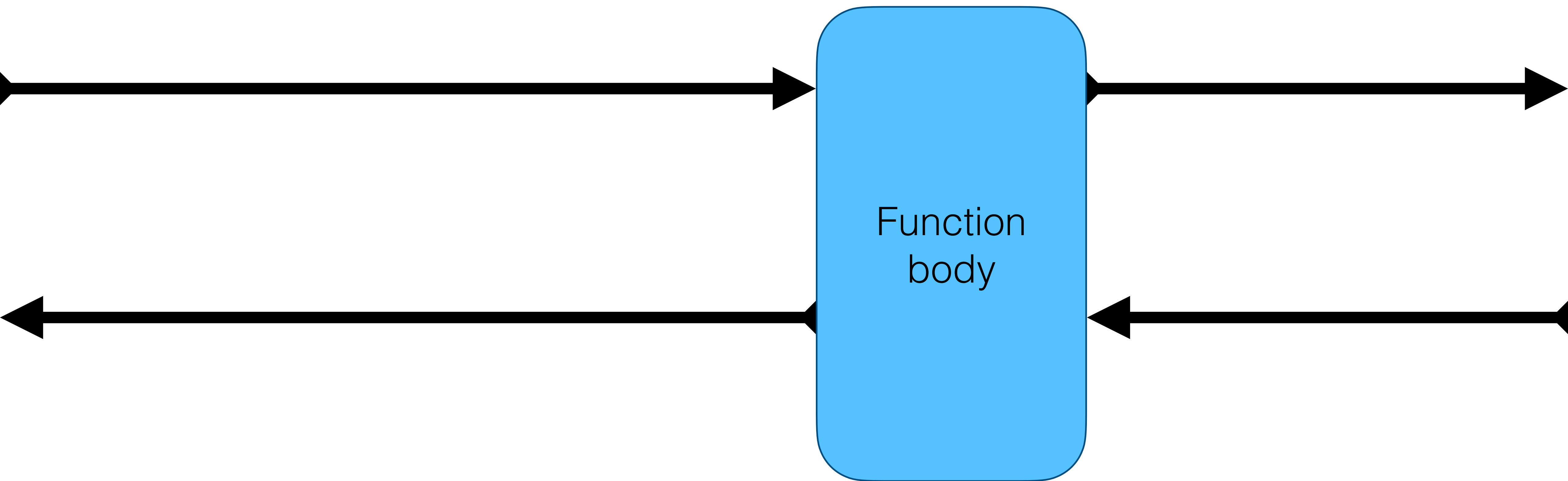






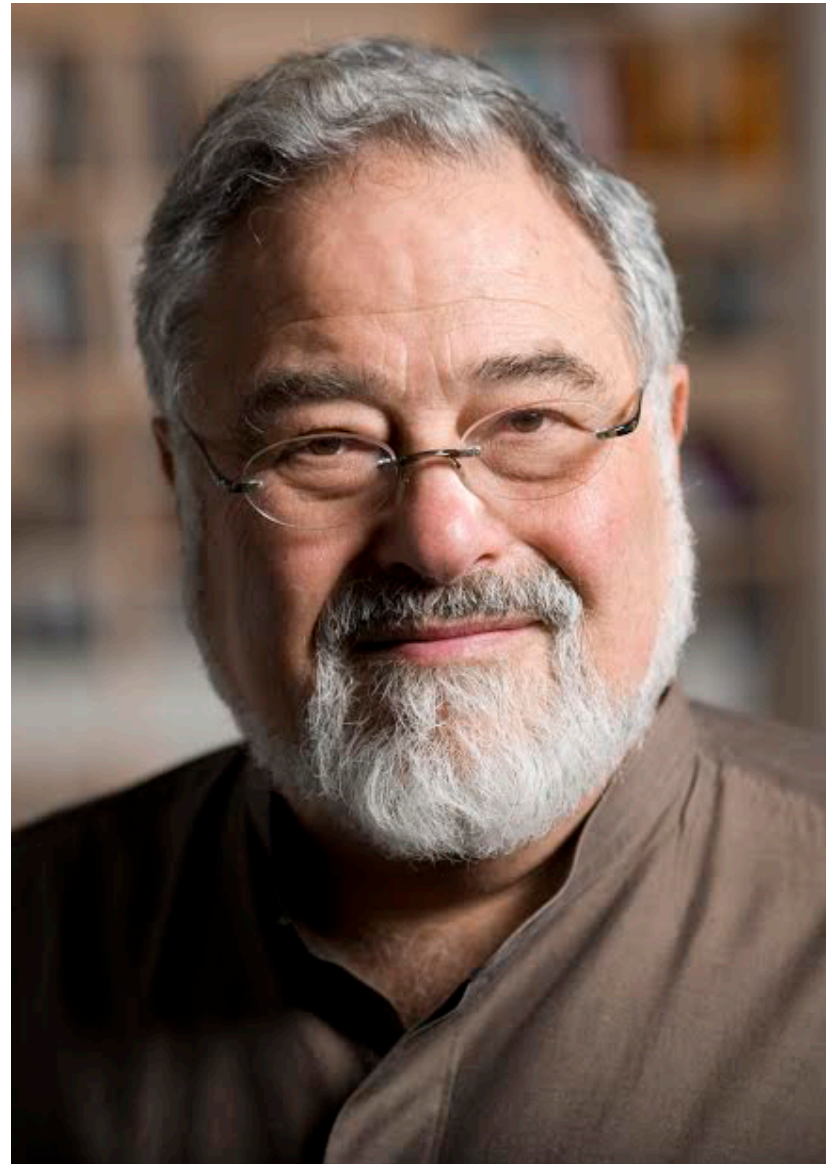






If your optimizer removes every ledger error path,
your function gets a gold star!





George Lakoff (1941-)

Metaphors We Live By
(with Mark Johnson)
University of Chicago Press, 1980

Where Mathematics Comes From
(with Rafael E. Núñez)
Basic Books, 2000

The world is rich with solutions.
A good metaphor lets us apply them.

Thank you for listening.

Questions?